



BEYOND EXCELLENCE - 50

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Where the extreme challenges excellence.

Show that

$$\int_0^{\pi/2} \ln(\sin x) dx = \int_0^{\pi/2} \ln(\cos x) dx = \frac{1}{2} \int_0^{\pi/2} \ln(\sin 2x) dx - \frac{\pi}{4} \ln 2 \text{ and}$$

$$\int_0^{\pi/2} \ln(\sin 2x) dx = \frac{1}{2} \int_0^{\pi} \ln(\sin x) dx = \int_0^{\pi/2} \ln(\sin x) dx$$

$$\text{Hence deduce that } \int_0^{\pi/2} \ln(\sin x) dx = \frac{\pi}{2} \ln \frac{1}{2}$$

$$\# \int_0^{\pi/2} \ln(\sin x) dx = \int_0^{\pi/2} \ln(\cos x) dx = \frac{1}{2} \int_0^{\pi/2} \ln(\sin 2x) dx - \frac{\pi}{4} \ln 2 \text{ බවත්}$$

$$\int_0^{\pi/2} \ln(\sin 2x) dx = \frac{1}{2} \int_0^{\pi} \ln(\sin x) dx = \int_0^{\pi/2} \ln(\sin x) dx \text{ බවත් පෙන්වන්න.}$$

$$\text{එනමින් } \int_0^{\pi/2} \ln(\sin x) dx = \frac{\pi}{2} \ln \frac{1}{2} \text{ බව පෙන්වන්න.}$$